

An optimal control approach to the high intensity interval training design

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Abstract

Introduction: Prediction of the acute response induced by various training protocols is of great importance when looking for a systematic approach in designing high intensity training (HIT) sessions. The prediction of some of the indexes of the metabolic load (e.g. pulmonary oxygen consumption ($VO_2(t)$, [mlO₂/min]), blood lactate concentration ([La_b], mM), anaerobic source depletion (AnS, [J])) induced by the mechanical load (i.e. the intensity of the exercise ($P(t)$, [W]), can rely on theoretical tools like mathematical models. The purpose of this study was twofold: 1) to develop a bioenergetic model of cycling best suited for an optimal control framework and 2) to use an optimal control algorithm (Bertolazzi2005) to predict the best combination of the parameters defining a HIT session (Buchheit2013).

Methods: We adapted the well-known MM 3-compartment model (Morton1986) for the optimal control application. The $VO_2(t)$, [La_b](t) and AnS(t) in response to a generic $P(t)$ was possible by means of the resulting system of differential equations. The model was calibrated and tested when tracking experimental data collected on a trained cyclist (PPO=300W, VO_{2max} =50mlO₂/min/kg) cycling on an indoor ergometer at different workloads. To evaluate the goodness of fit with actual data we calculated: the averaged value of residuals AvE, the Pearson's r and the R². The optimal control algorithm was asked to find the combination of the main parameters defining a HIT session (i.e. work interval time and intensity (t_w , [s] and P_w , [W]), recovery interval time and intensity (t_r , [s] and P_r , [W])) that, in n=5 bouts, total training time (t_t =32min) and anaerobic sources (AnS₀=22kJ), maximized the time spent above the 90% of VO_{2max} ($T@VO_{2max90\%}$, [min]).

Results: Model was capable to replicate with good accuracy the experimental data of $VO_2(t)$ and [La_b](t) in similar conditions ($r>0.85$, $R^2>0.65$, AvgE<SE), giving confidence in applying this model in the estimation of AnS(t). The optimal control algorithm suggested for a HIT session in which the work intervals are interspersed by recovery intervals with different time durations (see Fig. 1). We found that: $T@VO_{2max90\%}\approx 10$ min and $\%T@VO_{2max90\%}\approx 30\%$ with working intervals at 100%PVO_{2max} of ~3', 3:30", 2':20", 3':30", 3' interspersed by recovery intervals at light intensity of ~1':30", 3':30", 9', 1':30". Average simulated $P(t)$ was ~218 W.

Discussion: Simulated data are close to those reported in the literature for similar training protocols ($T@VO_{2max90\%}$, $\%T@VO_{2max90\%}$). The optimal control algorithm suggests that we can improve classical training protocols in which the working and recovery intervals are constant across the session. With individualized parameters it is possible to estimate the response of the athlete to the induced metabolic load and then to generate more time-efficient and more effective training sessions.

Conclusion: Mathematical models and optimal control can offer a valid contribution in a systematic approach to the HIT design in cycling as they can handle the complexity of parameters that usually show mutual interaction. To the best of our knowledge, there are no methods available in the literature that can systematically handle the problem of optimizing the HIT protocols. The method suggest moving towards protocol in which working and recovery time intervals are not constant across the exercise.



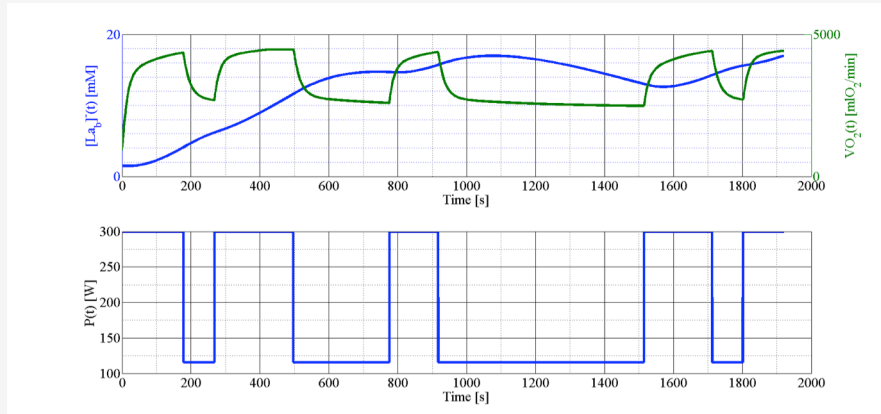


Figure 1: Suggested training protocol.

Keywords: High-Intensity-Training, cycling, mathematical models, optimal control

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